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3D Face Morphable Models “In-the-Wild”

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Abstract

3D Morphable Models (3DMMs) are powerful statistical models of 3D facial shape and texture, and among the state-of-the-art methods for reconstructing facial shape from single images. With the advent of new 3D sensors, many 3D facial datasets have been collected containing both neutral as well as expressive faces. However, all datasets are captured under controlled conditions. Thus, even though powerful 3D facial shape models can be learnt from such data, it is difficult to build statistical texture models that are sufficient to reconstruct faces captured in unconstrained conditions (“in-the-wild”). In this paper, we propose the first, to the best of our knowledge, “in-the-wild” 3DMM by combining a powerful statistical model of facial shape, which describes both identity and expression, with an “in-the-wild” texture model. We show that the employment of such an “in-the-wild” texture model greatly simplifies the fitting procedure, because there is no need to optimise with regards to the illumination parameters. Furthermore, we propose a new fast algorithm for fitting the 3DMM in arbitrary images. Finally, we have captured the first 3D facial database with relatively unconstrained conditions and report quantitative evaluations with state-of-the-art performance. Complementary qualitative reconstruction results are demonstrated on standard “in-the-wild” facial databases.

1. Introduction

During the past few years, we have witnessed significant improvements in various face analysis tasks such as face detection [19, 42] and 2D facial landmark localisation on static images [40, 21, 6, 38, 43, 4, 5, 36]. This is primarily attributed to the fact that the community has made a considerable effort to collect and annotate facial images captured under unconstrained conditions [24, 45, 9, 32, 31] (commonly referred to as “in-the-wild”) and to the discriminative methodologies that can capitalise on the availability of such large amount of data. Nevertheless, discriminative techniques cannot be applied for 3D facial shape estimation “in-the-wild”, due to lack of ground-truth data.

3D facial shape estimation from single images has attracted the attention of many researchers the past twenty years. The two main lines of research are (i) fitting a 3D Morphable Model (3DMM) [11, 12] and (ii) applying Shape from Shading (SfS) techniques [34, 35, 22]. The 3DMM fitting proposed in the work of Blanz and Vetter [11, 12] was among the first model-based 3D facial recovery approaches. The method requires the construction of a 3DMM which is a statistical model of facial texture and shape in a space where there are explicit correspondences. The first 3DMM was built using 200 faces captured in well-controlled conditions displaying only the neutral expression. That is the reason why the method was only shown to work on real-world, but not “in-the-wild”, images. State-of-the-art SfS techniques capitalise on special multi-linear decompositions that find an approximate spherical harmonic decomposition of the illumination. Furthermore, in order to benefit from the large
availability of “in-the-wild” images, these methods jointly reconstruct large collections of images. Nevertheless, even though the results of [34, 22] are quite interesting, given that there is no prior of the facial surface, the methods only recover 2.5D representations of the faces and particularly smooth approximations of the facial normals.

3D facial shape recovery from a single image under “in-the-wild” conditions is still an open and challenging problem in computer vision mainly due to the fact that:

• The general problem of extracting the 3D facial shape from a single image is an ill-posed problem which is notoriously difficult to solve without the use of any statistical priors for the shape and texture of faces. That is, without prior knowledge regarding the shape of the object at-hand there are inherent ambiguities present in the problem. The pixel intensity at a location in an image is the result of a complex combination of the underlying shape of the object, the surface albedo and normal characteristics, camera parameters and the arrangement of scene lighting and other objects in the scene. Hence, there are potentially infinite solutions to the problem.

• Learning statistical priors of 3D facial shape and texture for “in-the-wild” images is very difficult even using modern acquisition devices. That is, even though there is a considerable improvement in 3D acquisition devices, they still cannot operate in arbitrary conditions. Hence, all the current 3D facial databases have been captured in controlled conditions.

With the available 3D facial data, it is feasible to learn a powerful statistical model of the facial shape that generalises well for both identity and expression [14, 30, 13]. However, it is not possible to construct a statistical model of the facial texture that generalises well for “in-the-wild” images and is, at the same time, in correspondence with the statistical shape model. That is the reason why current state-of-the-art 3D face reconstruction methodologies rely solely on fitting a statistical 3D facial shape prior on a sparse set of landmarks [2, 16].

In this paper, we make a number of contributions that enable the use of 3DMMs for “in-the-wild” face reconstruction (Fig. 1). In particular, our contributions are:

• We propose a methodology for learning a statistical texture model from “in-the-wild” facial images, which is in full correspondence with a statistical shape prior that exhibits both identity and expression variations. Motivated by the success of feature-based (e.g., HOG [15], SIFT [25]) Active Appearance Models (AAMs) [3, 4] we further show how to learn feature-based texture models for 3DMMs. We show that the advantage of using the “in-the-wild” feature-based texture model is that the fitting strategy is much simplified since there is not need to optimise with respect to the illumination parameters.

• By capitalising on the recent advancements in fitting statistical deformable models [29, 37, 4, 1], we propose a novel and fast algorithm for fitting “in-the-wild” 3DMMs. Furthermore, we make the implementation of our algorithm publicly available, which we believe can be of great benefit to the community, given the lack of robust open-source implementations for fitting 3DMMs.

• Due to lack of ground-truth data, the majority of the 3D face reconstruction papers report only qualitative results. In this paper, in order to provide quantitative evaluations, we collected a new dataset of 3D facial surfaces, using Kinect Fusion [18, 28], which has many “in-the-wild” characteristics, even though it is captured indoors.

The remainder of the paper is structured as follows. In Section 2 we elaborate on the construction of our “in-the-wild” 3DMM, whilst in Section 3 we outline the proposed optimisation for fitting “in-the-wild” images with our model. Section 4 describes our new dataset, the first of its kind, to provide images with a ground-truth 3D facial shape that exhibit many “in-the-wild” characteristics. We outline a series of quantitative and qualitative experiments in Section 5, and end with conclusions in Section 6.

2. Model Training

A 3DMM consists of three parametric models: the shape, camera and texture models.

2.1. Shape Model

Let us denote the 3D mesh (shape) of an object with N vertexes as a $3N \times 1$ vector

$$s = [x_1^T, \ldots, x_N^T]^T = [x_1, y_1, z_1, \ldots, x_N, y_N, z_N]^T \tag{1}$$

where $x_i = [x_i, y_i, z_i]^T$ are the object-centered Cartesian coordinates of the i-th vertex. A 3D shape model can be constructed by first bringing a set of 3D training meshes into dense correspondence so that each is described with the same number of vertexes and all samples have a shared semantic ordering. The corresponded meshes, $\{s_i\}$, are then brought into a shape space by applying Generalized Procrustes Analysis and then Principal Component Analysis (PCA) is performed which results in $[\bar{s}, U_s]$, where $\bar{s} \in \mathbb{R}^{3N}$ is the mean shape vector and $U_s \in \mathbb{R}^{3N \times n_s}$ is the orthonormal basis after keeping the first $n_s$ principal components. This model can be used to generate novel 3D shape
instances using the function $S : \mathbb{R}^{n_s} \to \mathbb{R}^{3N}$ as

$$S(p) = \bar{s} + U_s p$$

(2)

where $p = [p_1, \ldots, p_{n_s}]^T$ are the $n_s$ shape parameters.

2.2. Camera Model

The purpose of the camera model is to map (project) the object-centered Cartesian coordinates of a 3D mesh instance $s$ into 2D Cartesian coordinates on an image plane. In this work, we employ a pinhole camera model, which utilizes a perspective transformation. However, an orthographic projection model can also be used in the same way.

**Perspective projection.** The projection of a 3D point $\mathbf{x} = [x, y, z]^T$ into its 2D location in the image plane $\mathbf{x}' = [x', y']^T$ involves two steps. First, the 3D point is rotated and translated using a linear view transformation, under the assumption that the camera is still

$$[v_x, v_y, v_z]^T = R_v \mathbf{x} + t_v$$

(3)

where $R_v \in \mathbb{R}^{3 \times 3}$ and $t_v = [t_x, t_y, t_z]^T$ are the 3D rotation and translation components, respectively. Then, a non-linear perspective transformation is applied as

$$\mathbf{x}' = \frac{f}{v_z} \begin{bmatrix} v_x \\ v_y \\ 1 \end{bmatrix} + \begin{bmatrix} c_x \\ c_y \end{bmatrix}$$

(4)

where $f$ is the focal length in pixel units (we assume that the $x$ and $y$ components of the focal length are equal) and $[c_x, c_y]^T$ is the principal point that is set to the image center.

**Quaternions.** We parametrise the 3D rotation with quaternions [23, 39]. The quaternion uses four parameters $q = [q_0, q_1, q_2, q_3]^T$ in order to express a 3D rotation as

$$R_q = 2 \begin{bmatrix} \frac{1}{2} - q_2^2 - q_3^2 & q_1 q_2 - q_0 q_3 & q_1 q_3 + q_0 q_2 \\ q_1 q_2 + q_0 q_3 & \frac{1}{2} - q_1^2 - q_3^2 & q_2 q_3 - q_0 q_1 \\ q_1 q_3 - q_0 q_2 & q_2 q_3 + q_0 q_1 & \frac{1}{2} - q_1^2 - q_2^2 \end{bmatrix}$$

(5)

Note that by enforcing a unit norm constraint on the quaternion vector, i.e. $q^T q = 1$, the rotation matrix constraints of orthogonality with unit determinant are withheld. Given the unit norm property, the quaternion can be seen as a three-parameter vector $[q_1, q_2, q_3]^T$ and a scalar $q_0 = \sqrt{1 - q_1^2 - q_2^2 - q_3^2}$. Most existing works on 3DMM parametrise the rotation matrix $R_q$ using the three Euler angles that define the rotations around the horizontal, vertical and camera axes. Even thought Euler angles are more naturally interpretable, they have strong disadvantages when employed within an optimisation procedure, most notably the solution ambiguity and the gimbal lock effect. Parametrisation based on quaternions overcomes these disadvantages and further ensures computational efficiency, robustness and simpler differentiation.

**Camera function.** The projection operation performed by the camera model of the 3DMM can be expressed with the function $P(s, c) : \mathbb{R}^{3N} \to \mathbb{R}^{2N}$, which applies the transformations of Eqs. 3 and 4 on the points of provided 3D mesh $s$ with

$$c = [f, q_1, q_2, q_3, t_x, t_y, t_z]^T$$

(6)

being the vector of camera parameters with length $n_c = 7$. For abbreviation purposes, we represent the camera model of the 3DMM with the function $W : \mathbb{R}^{n_s, n_c} \to \mathbb{R}^{2N}$ as

$$W(p, c) = P(S(p), c)$$

(7)

where $S(p)$ is a 3D mesh instance using Eq. 2.

2.3. “In-the-Wild” Feature-Based Texture Model

The generation of an “in-the-wild” texture model is a key component of the proposed 3DMM. To this end, we take advantage of the existing large facial “in-the-wild” databases that are annotated in terms of sparse landmarks. Assume that for a set of $M$ “in-the-wild” images $\{I_i\}_{i=1}^M$, we have access to the associated camera and shape parameters $\{p_i, c_i\}$. Let us also define a dense feature extraction function

$$F : \mathbb{R}^{H \times W} \to \mathbb{R}^{H \times W \times C}$$

(8)

where $C$ is the number of channels of the feature-based image. For each image, we first compute its feature-based representation as $F_i = F(I_i)$ and then use Eq. 7 to sample it at each vertex location to build back a vectorized texture sample $t_i = F_i(W(p_i, c_i)) \in \mathbb{R}^{C \times N}$. This texture sample will be nonsensical for some regions mainly due to self-occlusions present in the mesh projected in the image space.
For the 3D fits provided by using only the 2D landmarks [20], a texture model can be learned using the above procedure. This texture model used with the proposed 3DMM fitting algorithm on the same data establishes improved correspondences, refining the texture model.

3. Model Fitting

We propose to fit the 3DMM on an input image using a Gauss-Newton iterative optimisation. To this end, herein, we first formulate the cost function and then present two optimisation procedures.

3.1. Cost Function

The overall cost function of the proposed 3DMM formulation consists of a texture-based term, an optional error term based on sparse 2D landmarks, and an optional regularisation terms on the parameters.

**Texture reconstruction cost.** The main term of the optimisation problem is the one that aims to estimate the shape, texture and camera parameters that minimise the \( \ell_2^2 \) norm of the difference between the image feature-based texture that corresponds to the projected 2D locations of the 3D shape instance and the texture instance of the 3DMM. Let us denote by \( \mathbf{F} = \mathcal{F}(\mathbf{I}) \) the feature-based representation with \( C \) channels of an input image \( \mathbf{I} \) using Eq. 8. Then, the texture reconstruction cost is expressed as

\[
\arg \min_{p, c, \lambda} \| \mathbf{F} (\mathcal{W}(\mathbf{p}, c)) - \mathcal{T}(\lambda) \|^2
\]  

Note that \( \mathcal{W}(\mathbf{p}, c) \in \mathbb{R}^{CN} \) denotes the operation of sampling the feature-based input image on the projected 2D locations of the 3D shape instance acquired by the camera model (Eq. 7).

**Regularisation.** In order to avoid over-fitting effects, we augment the cost function with two optional regularisation terms over the shape and texture parameters. Let us denote as \( \Sigma_s \in \mathbb{R}^{n_s \times n_s} \) and \( \Sigma_t \in \mathbb{R}^{n_t \times n_t} \) the diagonal matrices with the eigenvalues in their main diagonal for the shape and texture models, respectively. Based on the PCA nature of the shape and texture models, it is assumed that their parameters follow normal prior distributions, i.e. \( p \sim \mathcal{N}(0, \Sigma_s) \) and \( \lambda \sim \mathcal{N}(0, \Sigma_t) \). We formulate the regularisation terms as the \( \ell_2^2 \) of the parameters’ vectors weighted with the corresponding inverse eigenvalues, i.e.

\[
\arg \min_{p, \lambda} c_s \| p \|_{\Sigma_s^{-1}}^2 + c_t \| \lambda \|_{\Sigma_t^{-1}}^2
\]

where \( c_s \) and \( c_t \) are constants that weight the contribution of the regularisation terms in the cost function.

**2D landmarks cost.** In order to rapidly adapt the camera parameters in the cost of Eq. 11, we further expand the optimisation problem with the term

\[
\arg \min_{p, c} c_l \| \mathcal{W}_l (\mathbf{p}, c) - s_l \|^2
\]
where \( s_l = [x_l, y_l, \ldots, x_L, y_L]^T \) denotes a set of \( L \) sparse 2D landmark points (\( L \ll N \)) defined on the image coordinate system and \( W_l(p, c) \) returns the \( 2L \times 1 \) vector of 2D projected locations of these \( L \) sparse landmarks. Intuitively, this term aims to drive the optimisation procedure using the selected sparse landmarks as anchors for which we have the optimal locations \( s_l \). This optional landmarks-based cost is weighted with the constant \( c_l \).

**Overall cost function.** The overall 3DMM cost function is formulated as the sum of the terms in Eqs. 11, 12, 13, i.e.

\[
\arg\min_{p, c, \lambda} ||F(W(p, c)) - T(\lambda)||^2 + c_l ||W_l(p, c) - s_l||^2 +
+ c_s ||p||^2_{\Sigma^{-1}} + c_t ||\lambda||^2_{\Sigma^{-1}}.
\]  

(14)

The landmarks term as well as the regularisation terms are optional and aim to guide the optimisation procedure to converge faster and to a better minimum. Note that thanks to the proposed “in-the-wild” feature-based texture model, the cost function does not include any parametric illumination model similar to the ones in the relative literature [11, 12], which greatly simplifies the optimisation.

**3.2. Gauss-Newton Optimisation**

Inspired by the extensive literature in Lucas-Kanade 2D image alignment [7, 27, 29, 37, 4, 1], we formulate a Gauss-Newton optimisation framework. Specifically, given that the camera projection model is applied on the image part of Eq. 14, the proposed optimisation has a “forward” nature.

**Parameters update.** The shape, texture and camera parameters are updated in an additive manner, i.e.

\[
p \leftarrow p + \Delta p, \quad \lambda \leftarrow \lambda + \Delta \lambda, \quad c \leftarrow c + \Delta c
\]  

(15)

where \( \Delta p \), \( \Delta \lambda \) and \( \Delta c \) are their increments estimated at each fitting iteration. Note that in the case of the quaternion used to parameterise the 3D rotation matrix, the update is performed as the multiplication

\[
q \leftarrow (\Delta q)q = \begin{bmatrix} \Delta q_0 \\ \Delta q_{1:3} \end{bmatrix} =
\begin{bmatrix} q_0 \\ q_{1:3} \end{bmatrix} +
\begin{bmatrix} q_0 \\ \Delta q_{1:3} \end{bmatrix}
\]  

(16)

\[
= \begin{bmatrix} \Delta q_0q_0 - \Delta q_{1:3}^Tq_{1:3} \\ \Delta q_0q_{1:3} + q_0q_{1:3} + \Delta q_{1:3} \times q_{1:3} \end{bmatrix}
\]

However, we will still denote it as an addition for simplicity. Finally, we found that it is beneficial to keep the focal length constant in most cases, due to its ambiguity with \( t_z \).

**Linearisation.** By introducing the additive incremental updates on the parameters of Eq. 14, the cost function is expressed as

\[
\arg\min_{\Delta p, \Delta c, \Delta \lambda} ||F(W(p + \Delta p, c + \Delta c)) - T(\lambda + \Delta \lambda)||^2 +
+ c_l ||W_l(p + \Delta p, c + \Delta c) - s_l||^2 +
+ c_s ||p + \Delta p||^2_{\Sigma^{-1}} + c_t ||\lambda + \Delta \lambda||^2_{\Sigma^{-1}}
\]  

(17)

Note that the texture reconstruction and landmarks constraint terms of this cost function are non-linear due to the camera model operation. We need to linearised them around \((p, c)\) using first order Taylor series expansion at \((p + \Delta p, c + \Delta c) = (p, c) \Rightarrow (\Delta p, \Delta c) = 0\). The linearisation for the image term gives

\[
F(W(p + \Delta p, c + \Delta c)) \approx F(W(p, c)) +
+ J_{F,p} \Delta p + J_{F,c} \Delta c
\]  

(18)

where \( J_{F,p} = \nabla F \frac{\partial W}{\partial p} \bigg|_{p=p} \) and \( J_{F,c} = \nabla F \frac{\partial W}{\partial c} \bigg|_{c=c} \) are the image Jacobians with respect to the shape and camera parameters, respectively. Note that most dense feature-extraction functions \( F(\cdot) \) are non-differentiable, thus we simply compute the gradient of the multi-channel feature image \( \nabla F \). Similarly, linearisation of the sparse landmarks projection term gives

\[
W_l(p + \Delta p, c + \Delta c) \approx W_l(p, c) + J_{W_l,p} \Delta p + J_{W_l,c} \Delta c
\]  

(19)

where \( J_{W_l,p} = \frac{\partial W_l}{\partial p} \bigg|_{p=p} \) and \( J_{W_l,c} = \frac{\partial W_l}{\partial c} \bigg|_{c=c} \) are the camera Jacobians. Please refer to the supplementary material for more details on the computation of these derivatives.

**3.2.1 Simultaneous**

Herein, we aim to simultaneously solve for all parameters’ increments. By substituting Eqs. 18 and 19 in Eq. 17 we get

\[
\arg\min_{\Delta p, \Delta c, \Delta \lambda} ||F(W(p, c)) + J_{F,p} \Delta p + J_{F,c} \Delta c - T(\lambda + \Delta \lambda)||^2 +
+ c_l ||W_l(p, c) + J_{W_l,p} \Delta p + J_{W_l,c} \Delta c - s_l||^2 +
+ c_s ||p + \Delta p||^2_{\Sigma^{-1}} + c_t ||\lambda + \Delta \lambda||^2_{\Sigma^{-1}}
\]

(20)

Let us concatenate the parameters and their increments as \( b = [p^T, c^T, \lambda^T]^T \) and \( \Delta b = [\Delta p^T, \Delta c^T, \Delta \lambda^T]^T \). By taking the derivative of the final linearised cost function with respect to \( \Delta b \) and equalising with zero, we get the solution

\[
b = -H^{-1}(J_F^T e_F + c_t J_{W_l} e_l + c_s \Sigma_{-1}^{-1} p + c_t \Sigma_{-1}^{-1} \lambda)
\]

(21)

where \( H = J_F^T J_F + c_t J_{W_l}^T J_{W_l} + c_s \Sigma_{-1}^{-1} + c_t \Sigma_{-1}^{-1} \) is the Hessian with

\[
J_F = \begin{bmatrix} J_{F,p}^T \\ J_{F,c}^T \\ -U_l^T \end{bmatrix}^T
\]

(22)

\[
J_{W_l} = \begin{bmatrix} J_{W_l,p}^T \\ J_{W_l,c}^T \\ 0_{n_t \times 2L} \end{bmatrix}^T
\]

\[
e_F = F(W(p, c)) - T(\lambda)
\]

\[
e_l = W_l(p, c) - s_l
\]

(23)
are the residual terms. The computational complexity of the Simultaneous algorithm per iteration is dominated by the texture reconstruction term as $O((n_s + n_c + n_t)^3 + CN(n_s + n_c + n_t)^2)$, which in practice is too slow.

### 3.2.2 Project-Out

We propose to use a Project-Out optimisation approach that is much faster than the Simultaneous. The main idea is to optimise on the orthogonal complement of the texture subspace which will eliminate the need to solve for the texture parameters increment at each iteration. By substituting Eqs. 18 and 19 into Eq. 17 and removing the incremental update on the texture parameters as well as the texture parameters regularisation term, we end up with the problem

$$
\arg \min_{\Delta p, \Delta c, \lambda} \left\| F(W(p, c)) + J_{F,p} \Delta p + J_{F,c} \Delta c - T(\lambda) \right\|^2 + \\
+ c_t \left\| W_i(p, c) + J_{W_i,p} \Delta p + J_{W_i,c} \Delta c - s_i \right\|^2 + \\
+ c_s \left\| p + \Delta p \right\|^2_{\Sigma_s^{-1}}
$$

The solution of Eq. 24 with respect to $\lambda$ is readily given by

$$
\lambda = U^T \left( F(W(p, c)) + J_{F,p} \Delta p + J_{F,c} \Delta c - \bar{t} \right)
$$

By plugging Eq. 25 into Eq. 24, we get

$$
\arg \min_{\Delta p, \Delta c} \left\| F(W(p, c)) + J_{F,p} \Delta p + J_{F,c} \Delta c - \bar{t} \right\|^2_{p} + \\
+ c_t \left\| W_i(p, c) + J_{W_i,p} \Delta p + J_{W_i,c} \Delta c - s_i \right\|^2 + \\
+ c_s \left\| p + \Delta p \right\|^2_{\Sigma_s^{-1}}
$$

where $P = E - U_t U_t^T$ is the orthogonal complement of the texture subspace that functions as the "project-out" operator with $E$ denoting the $CN \times CN$ unitary matrix. Note that in order to derive Eq. 26, we use the properties $P^T = P$ and $P^T P = P$. By differentiating Eq. 26 and equalizing to zero, we get the solution

$$
\Delta p = H_p^{-1} (J_{F,p}^T P e_F + c_t J_{W_i,p}^T e_t + c_s \Sigma_s^{-1} p) \\
\Delta c = H_c^{-1} (J_{F,c}^T P e_F + c_t J_{W_i,c}^T e_t)
$$

where

$$
H_p = J_{F,p}^T P J_{F,p} + c_t J_{W_i,p}^T J_{W_i,p} + c_s \Sigma_s^{-1} \\
H_c = J_{F,c}^T P J_{F,c} + c_t J_{W_i,c}^T J_{W_i,c}
$$

are the Hessian matrices and

$$
e_F = F(W(p, c)) - \bar{t} \\
e_t = W_i(p, c) - s_i
$$

are the residual terms. The texture parameters can be estimated at the end of the iterative procedure using Eq. 25.

Note that the most expensive operation is $J_{F,p}^T P$. However, if we first do $J_{F,p}^T U$ and then multiply this result with $U^T$, the total cost becomes $O(CNn_t n_s)$. The same stands for $J_{F,c}^T P$. Consequently, the cost per iteration is $O((n_s + n_c)^3 + CNn_t(n_s + n_c) + CN(n_s + n_c)^2)$ which is much faster than the Simultaneous algorithm.

**Residual masking**. In practice, we apply a mask on the texture reconstruction residual of the Gauss-Newton optimisation, in order to speed-up the 3DMM fitting. This mask is constructed by first acquiring the set of visible vertexes using z-buffering and then randomly selecting $K$ of them. By keeping the number of vertexes small ($K \approx 5000 \ll N$), we manage to greatly speed-up the fitting process without any accuracy penalty.

### 4. KF-ITW Dataset

For the evaluation of the 3DMM, we have constructed KF-ITW, the first dataset of 3D faces captured under relatively unconstrained conditions. The dataset consists of 17 different subjects recorded under various illumination conditions performing a range of expressions (neutral, happy, surprise). We employed the KinectFusion [18, 28] framework to acquire a 3D representation of the subjects with a Kinect v1 sensor.

The fused mesh for each subject serves as a 3D face ground-truth in which we can evaluate our algorithm and compare it to other methods. A voxel grid of size $608^3$ was utilised to get the detailed 3D scans of the faces. In order to accurately reconstruct the entire surface of the faces, a circular motion scanning pattern was carried out. Each subject was instructed to stay still in a fixed pose during the entire scanning process. The frame rate for every subject was constant to 8 frames per second. After getting the 3D scans from the KinectFusion framework we fit our shape model in a non-rigid manner to get a clean mesh with a distinct number of vertexes for the evaluation process. Finally, each mesh was manually annotated with the iBUG 49 sparse landmark set.

### 5. Experiments

To train our model, which we label as ITW, we use a variant of the Basel Face Model (BFM) [30] that we trained to contain both identities drawn from the original BFM model along with expressions provided by [14]. We trained the “in-the-wild” texture model on the images of iBUG, LFPMW & AFW datasets [31] as described in Sec. 2.3 using the 3D shape fits provided by [44]. Additionally, we elect to use the project-out formulation for the throughout our experiments due its superior run-time performance and equivalent fitting performance to the simultaneous one.
5.1. 3D Shape Recovery

Herein, we evaluate our “in-the-wild” 3DMM (ITW) in terms of 3D shape estimation accuracy against two popular state-of-the-art alternative 3DMM formulations. The first one is a classic 3DMM with the original Basel laboratory texture model and full lighting equation which we term Classic. The second is the texture-less linear model proposed in [16, 17] which we refer to as Linear. For Linear code we use the Surrey Model with related blendshapes along with the implementation given in [17].

We use the ground-truth annotations provided in the KF-ITW dataset to initialize and fit all three techniques to the “in-the-wild” style images in the dataset. The mean mesh of each model under test is landmarked with the same 49-point markup used in the dataset, and is registered against the ground truth mesh by performing a Procrustes alignment using the sparse annotations followed by Non-Rigid Iterative Closest Point (N-ICP) to iteratively deform the two surfaces until they are brought into correspondence. This provides a per-model ‘ground-truth’ for the 3D shape recovery problem for each image under test. Our error metric is the per-vertex dense error between the recovered shape and the model-specific corresponded ground-truth fit, normalized by the inter-ocular distance for the test mesh. Fig. 4 shows the cumulative error distribution for this experiment for the three models under test. Table 1 reports the corresponding Area Under the Curve (AUC) and failure rates. The Classic model struggles to fit to the “in-the-wild” conditions present in the test set, and performs the worst. The texture-free Linear model does better, but the ITW model is most able to recover the facial shapes due to its ideal feature basis for the “in-the-wild” conditions.

Figure 6 demonstrates qualitative results on a wide range of fits of “in-the-wild” images drawn from the Helen and 300W datasets [31, 32] that qualitatively highlight the effectiveness of the proposed technique. We note that in a wide variety of expression, identity, lighting and occlusion conditions our model is able to robustly reconstruct a realistic 3D facial shape that stands up to scrutiny.

5.2. Quantitative Normal Recovery

As a second evaluation, we use our technique to find per-pixel normals and compare against two well established Shape-from-Shading (SfS) techniques: PS-NL [8] and IMM [22]. For experimental evaluation we employ images of 100 subjects from the Photoface database [41]. As a set of four illumination conditions are provided for each subject then we can generate ground-truth facial surface normals using calibrated 4-source Photometric Stereo [26]. In Fig. 5 we show the cumulative error distribution in terms of the mean angular error. ITW slightly outperforms IMM even though both IMM and PS-NL use all four available images of each subject.

6. Conclusion

We have presented a novel formulation of 3DMMs re-imagined for use in “in-the-wild” conditions. We capitalise on the annotated “in-the-wild” facial databases to propose a methodology for learning an “in-the-wild” feature-based texture model suitable for 3DMM fitting without having to optimise for illumination parameters. Furthermore, we propose a novel optimisation procedure for 3DMM fitting. We
show that we are able to recover shapes with more detail than is possible using purely landmark-driven approaches. Our newly introduced “in-the-wild” KinectFusion dataset allows for the first time a quantitative evaluation of 3D facial reconstruction techniques in the wild, and on these evaluations we demonstrate that our in the wild formulation is state of the art, outperforming classical 3DMM approaches by a considerable margin.

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